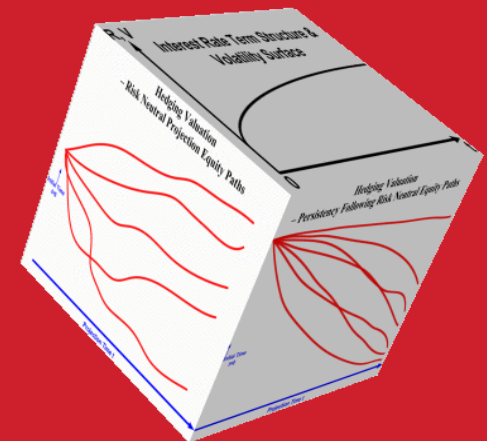


# Traditional, investment, and risk management actuaries in the life insurance industry

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- Traditional insurance products and investment actuaries**
- Variable annuities and financial engineering
- Critical skills, education and knowledge needed as an actuary

# Life insurance products

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- ❑ Traditional insurance products with protections for mortality, longevity, morbidity, etc. may be diversified
  
- ❑ Life insurance products
  - ⇒ Life insurance – paid on death as wealth protection
  - ⇒ Annuity – asset accumulation with tax deferral as investment for retirement
  
- ❑ Life insurance companies are assets rich
  - ⇒ Customers deposit money to insurance companies
  - ⇒ Insurance companies invest prudently for the long term
  - ⇒ Insurance pay the claims many years down the road
  - ⇒ Safety is critical



# Life actuaries – Traditional actuaries

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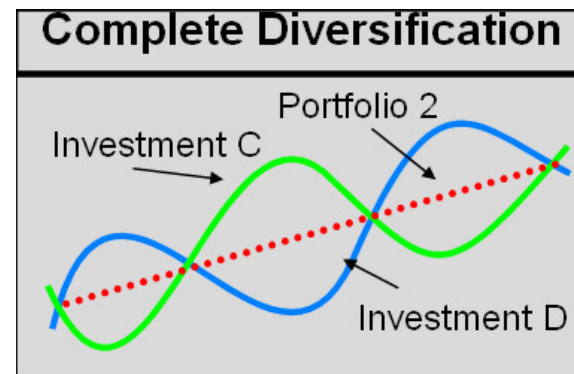
- ❑ Product pricing (engineers of the insurance company)
  - ⇒ To design products that generate economic value and have long-term profitability
  - ⇒ Need to be creative
  - ⇒ Responsible for profitable products
  - ⇒ Communication with sales and marketing
  
- ❑ Financial valuation and reporting
  - ⇒ To value and report insurance liabilities sold
  - ⇒ Need to be conservative
  - ⇒ Working closely with accounting and finance staff
  - ⇒ Not accountants but typically more knowledgeable than accountants on insurance liabilities (products)

# Life insurance is based on diversification

- Most products can be safely priced based on actuarial expected values (averages) and standard deviation



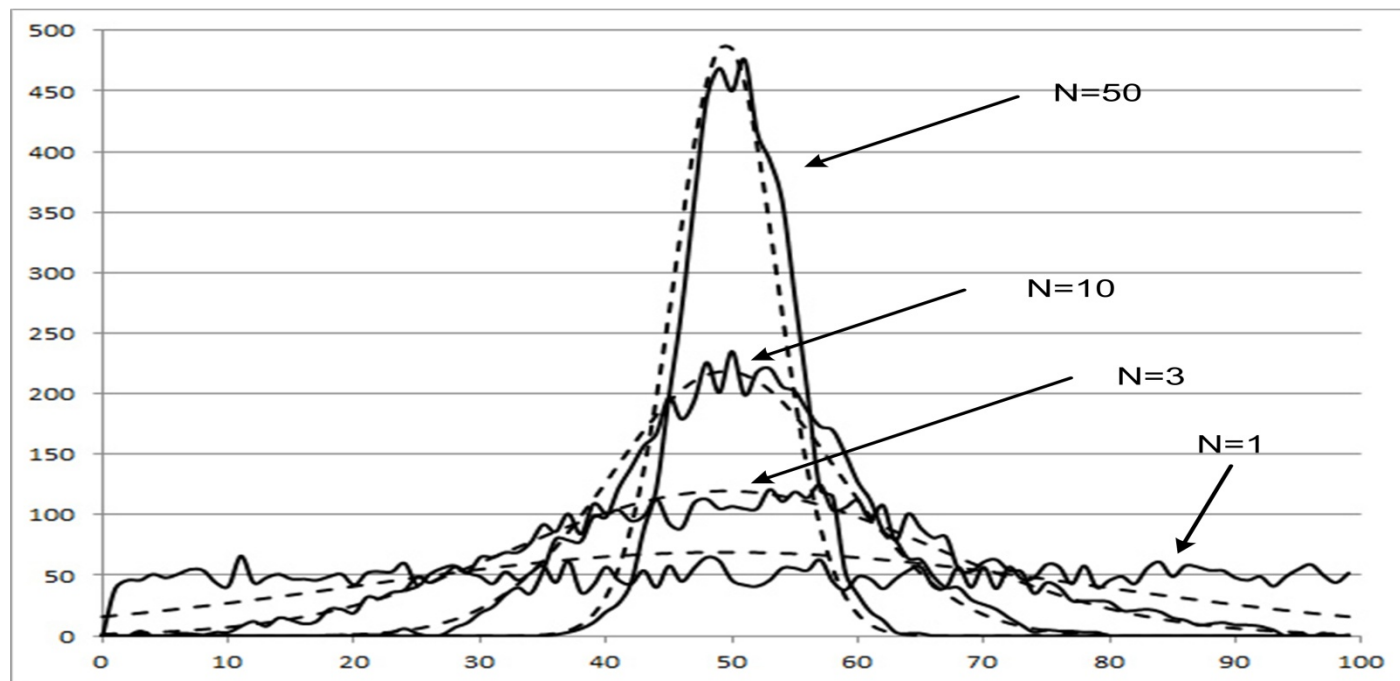
- The power of diversification



- The risk of systemic exposure

# Law of large numbers

- ❑ To reduce the uncertainty (risk or standard deviation) of the expected outcome
  - ⇒ **Sell a large number of small amount of insurance**
  
- ❑ The old and true statistical principle of “**law of large numbers**”
  - ⇒ Statistically speaking, larger samples reduce “sample error”



# Actuaries are engineers in insurance companies

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- ❑ Actuaries develop the tools used to build the insurance products (not widgets)
- ❑ Actuarial tools are financial models (not machine tools)
- ❑ Financial modeling is like computer game of financial cash flows (not soldiers and arms)
  - ⇒ Using software to model the events and activities
  - ⇒ Objects are financial cash flows (initial cash received and invested and later claims paid)
  - ⇒ Cash flows are simulated and analyzed
  - ⇒ Analysis focus on profitability (averages) and risks (tails)





# Actuarial modeling

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- ❑ All actuarial modeling work is on computer
  - ⇒ Widespread use of Excel spreadsheet models
  - ⇒ Some specialized actuarial software
  - ⇒ Extensive use of computer programming and database software
  - ⇒ All insurance products and their projected financials are modeled
  - ⇒ Based on actuarial and economic assumptions
  - ⇒ However, actuaries are not programmers – Programming is a tool for actuaries



# Investment and risk management actuaries

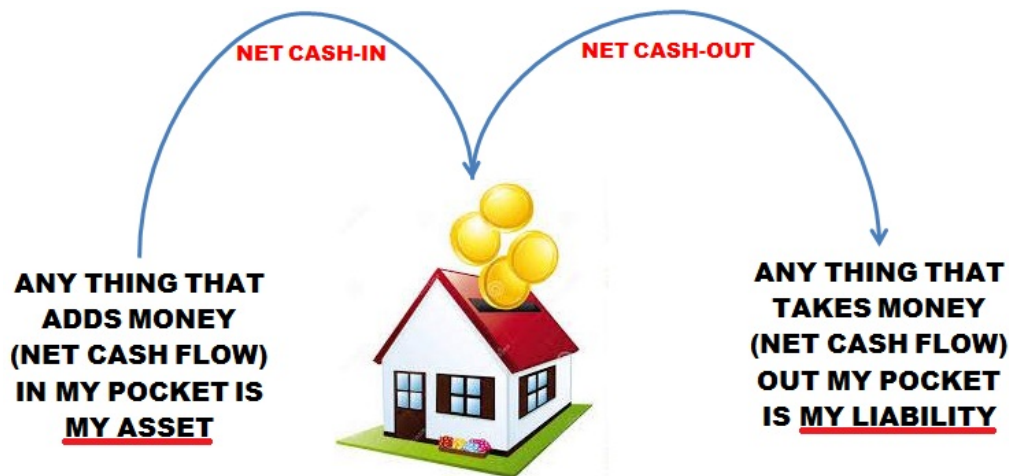
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- ❑ Life actuaries – Investment and risk management
  - ⇒ Most life insurance and annuity products have long term obligations (liabilities)
  - ⇒ Insurance companies are cash rich and big investors
  - ⇒ Insurance companies invest the monies received to pay for future claims
  
- ❑ Investment
  - ⇒ Most insurance company investments are in fixed income assets (bonds)
  - ⇒ Most insurance company liabilities are also long term fixed income in nature



# Asset liability management

- ❑ Investments by insurance companies need to provide both solid returns to support the future claims, business profits, and high degree of safety if things go wrong
  
- ❑ Asset liability management (ALM)
  - ⇒ Need to work with both actuarial insurance liabilities and portfolio investments
  - ⇒ ALM is art and science to balance assets and liabilities
  - ⇒ Actuaries doing ALM are “investment actuaries”
  - ⇒ Net asset and liability exposures to interest rate are immunized
    - Portfolios are managed with limited exposure to large interest rate moves (either up or down)



# Investment knowledge for ALM

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- ❑ Finance and investment knowledge
  - ⇒ Investment knowledge has been the core of actuarial science
  - ⇒ Actuaries work closely with portfolio managers (mostly fixed income investments)
  - ⇒ Actuaries can model sophisticated investment assets and their interactions with market interest rate drivers



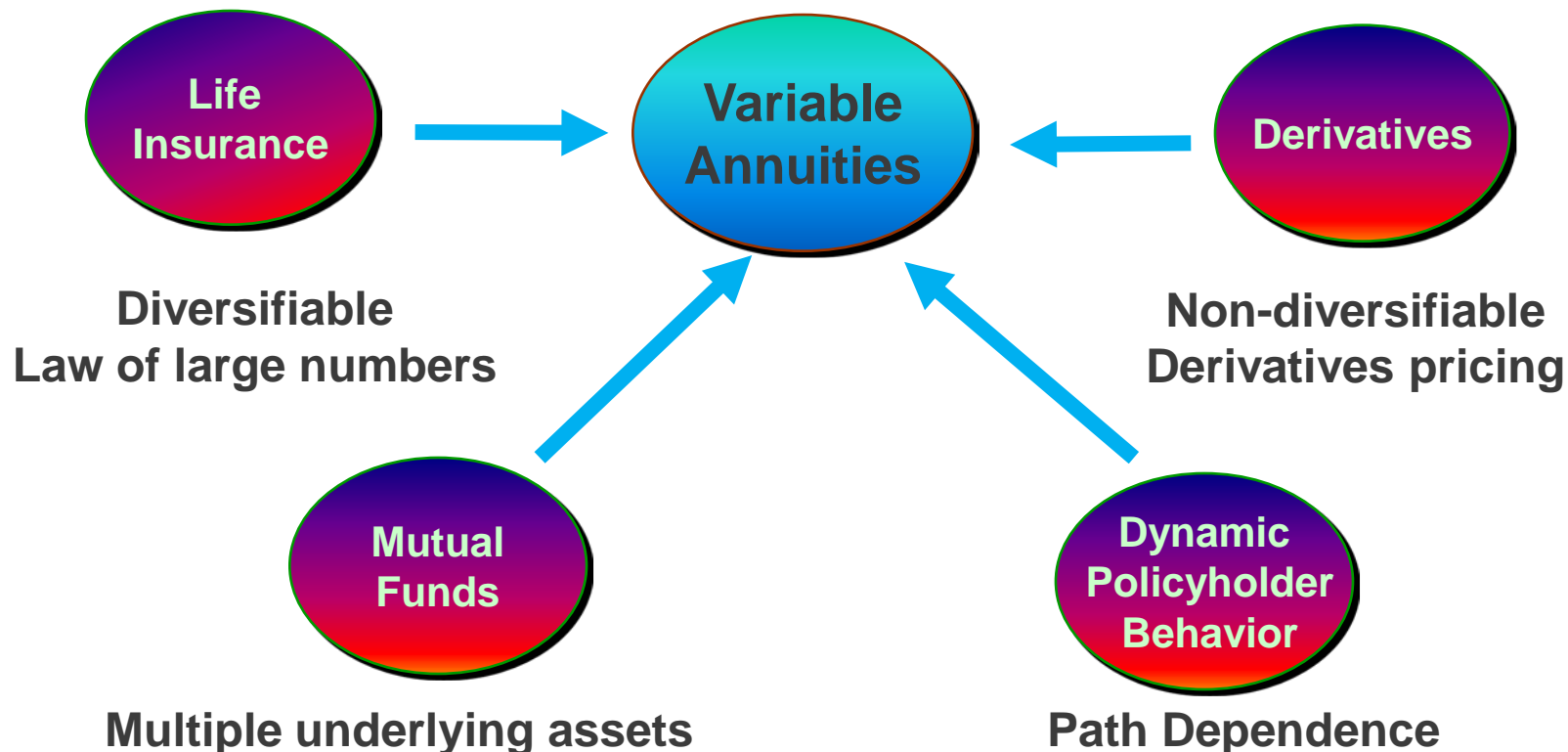
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- ❑ Traditional insurance products and investment actuaries
- ❑ **Variable annuities and financial engineering**
- ❑ Critical skills, education and knowledge needed as an actuary

# Life insurance or derivatives?

Variable annuity (VA) guarantees blur the boundary between derivatives products and traditional life insurance products: **Living or dying!**



VA contracts invest in mutual funds, paying fees to insurer, and getting guarantee benefits  
**GMDB (Guaranteed Minimum Death Benefit) => Payable at death**  
**VAGLB (Variable Annuity Guaranteed Living Benefit) => Payable Under Predefined Conditions:**  
 GMAB (Guaranteed Minimum Accumulation Benefit) for account value guarantee  
 GMIB (Guaranteed Minimum Income Benefit) for annuitized payouts guarantee  
 GMWB (Guaranteed Minimum Withdrawal Benefit) for withdrawals guarantee

# Sample VA GMDB designs

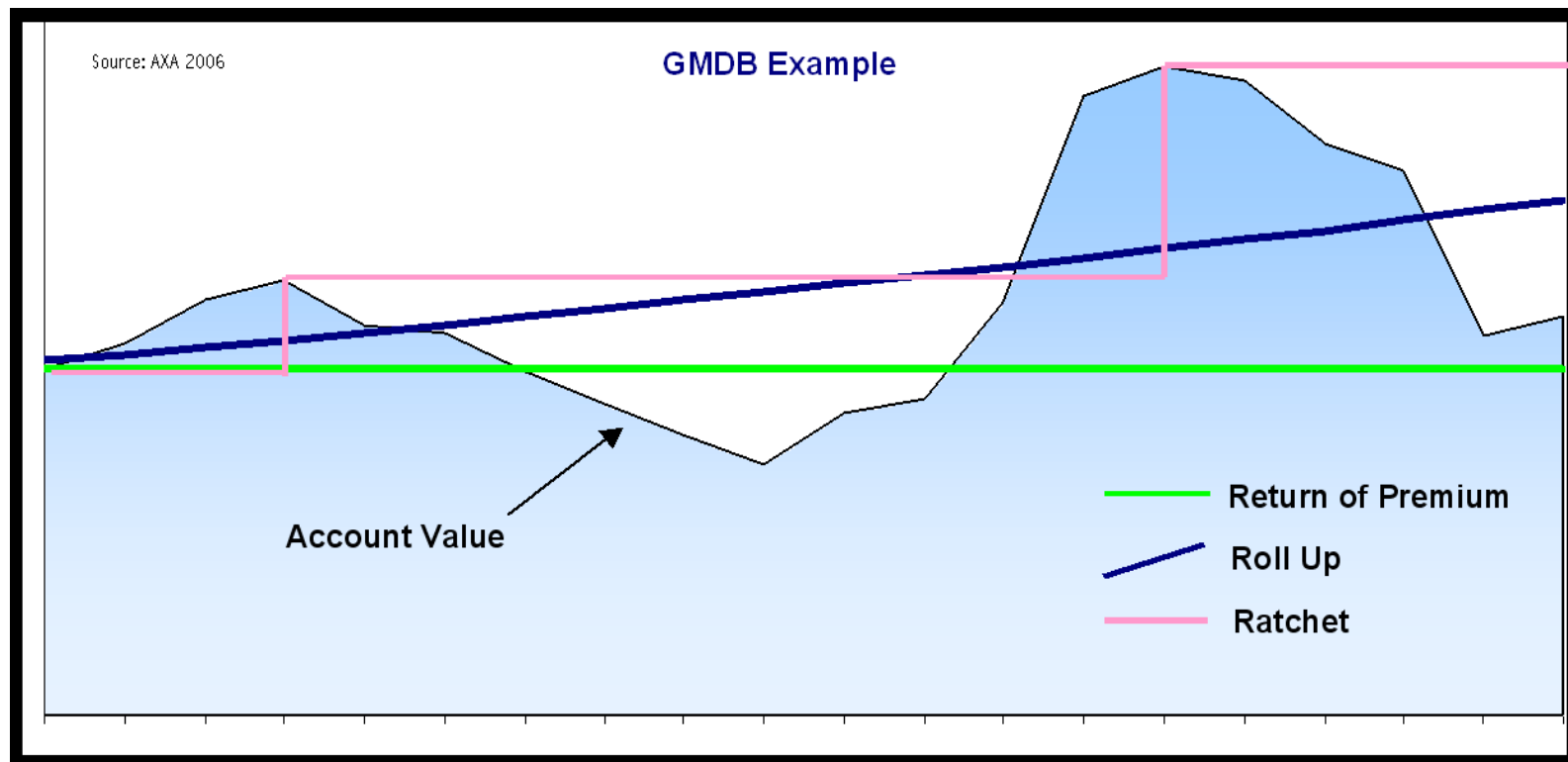
## □ Different strikes for different designs

**Return of premium:** strike = initial AV = initial premium deposits

**Ratchet:** discrete look back strike = max (sample AVs during the contract life)

**Rollup:** increasing strikes at an annual rate  $x$ : strike  $_t = (1+x)^t$

**Combinations:** strike = max of ratchet and rollup

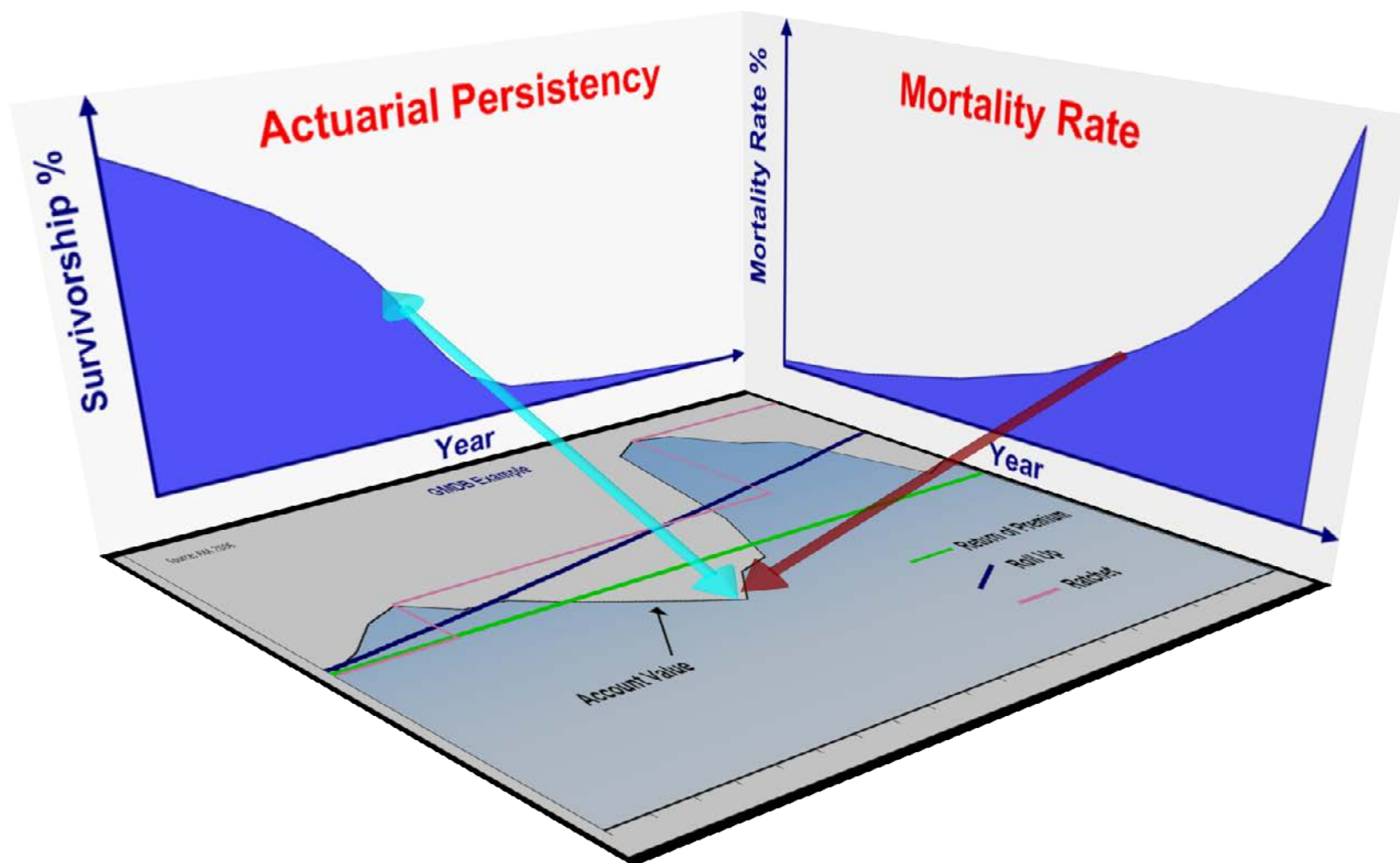


# How to price VA embedded derivatives

Risk neutral valuation using stochastic simulations

GMDB is paid only if GMDB is in the money and still In force at death

Price = sum of all future possible death payoffs on surviving contracts (by simulations)





# Capital market risk management

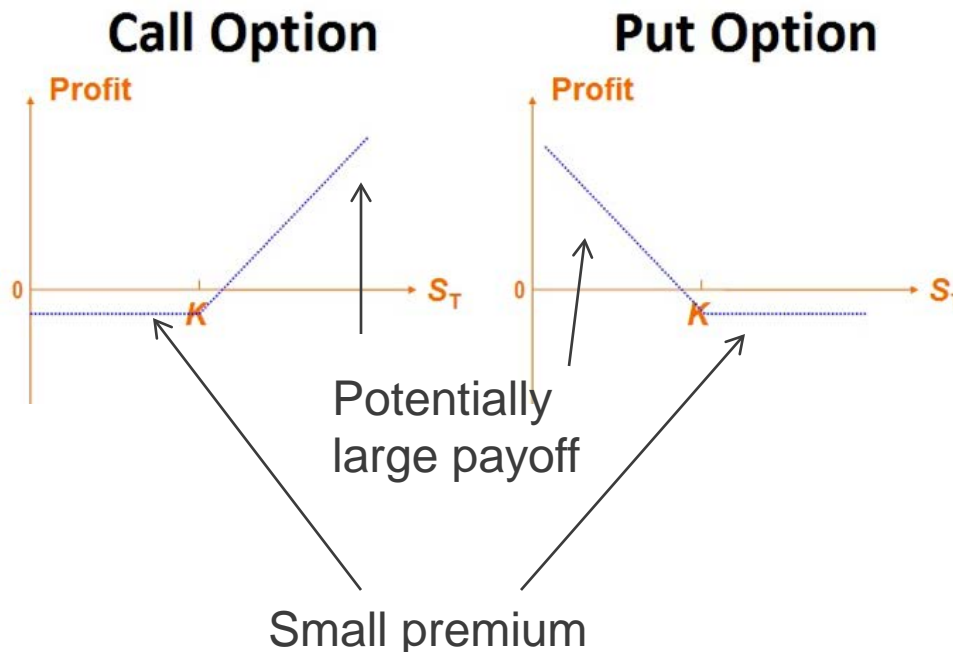
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- ❑ Capital markets are typically represented by Wall Street and portfolio investments
  
- ❑ Traditional investments in fixed income (bonds), equity (stocks), and modern derivatives (options)
  - ⇒ Fixed income portfolio management focuses on interest rate risk and credit risk
  - ⇒ Equity investment focuses on systematic risk (measured by beta)
  - ⇒ Derivatives are priced using financial engineering techniques
  
- ❑ Financial engineering is based on “law of one number” or no arbitrage
  
- ❑ Wall Street has used financial engineering to price and manage the risks for derivatives



# Derivatives, VA and fixed indexed annuities

- ❑ Options are capital market instruments
- ❑ Puts and calls have non-linear payoffs
  - ⇒ Only when stock price ends below or higher than the put/call strike respectively
  - ⇒ The options are highly leveraged with small option premium for potentially large payoffs
- ❑ VA writers sold short put options in GMDB and VAGLB as embedded benefits
- ❑ Fixed indexed annuity (FIA) writers sold short of call/call spread options



# Not all things can be averaged



Source: Simon Proctor

# Capital market law of one number (price)

- ❑ Financial engineering is based on “law of one number” or no arbitrage
- ❑ No arbitrage means no risk-free way of making money and there is only one price that is the market price



# Capital market one price – Risk neutral valuation

- ❑ Derivatives can be replicated **using** risk free instruments
- ❑ It turns out risk neutral pricing is a **very convenient trick** to **simplify derivatives** calculations
- ❑ Risk neutral replications is dynamic hedging
- ❑ Derivatives pricing using risk neutral does NOT assume risk free market outside this mathematical exercise

## The Black-Scholes Formula

$$C = S_0 \Phi \left[ \frac{\ln \left( \frac{S_0}{K} \right) + \left( r + \frac{1}{2} \sigma^2 \right) n}{\sigma \sqrt{n}} \right] - K e^{-rn} \Phi \left[ \frac{\ln \left( \frac{S_0}{K} \right) + \left( r - \frac{1}{2} \sigma^2 \right) n}{\sigma \sqrt{n}} \right]$$

*Martingale or risk neutral measure:  $H_t = E_Q(H_T | F_t)$*

*Girsanov theorem and Radon-Nikodym derivative:*

*Relationship between risk neutral and real world measures*



# Derivatives cannot be diversified

## ❑ Diversification by derivatives product offering is very limited

- ⇒ Shorting 100,000 put options with varying strikes and maturity dates
  - Add, but not reduce, the main exposure to the block – systemic exposure to equity
- ⇒ Selling VA and FIA
  - Might offset to some degree of the directional exposure to equity but not the volatility

## ❑ Derivatives risks are systemic

- ⇒ Time diversification is not very reliable – still the same market exposure



# Derivatives are hedged but not diversified

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## ❑ Sound risk management practice is

- ⇒ To neutralize the systemic capital market exposure by **hedging** (hope we have priced adequately)
- ⇒ The best “diversification” for derivatives is hedging

## ❑ Hedging with risk neutral valuation is the most reliable way to offload the risks

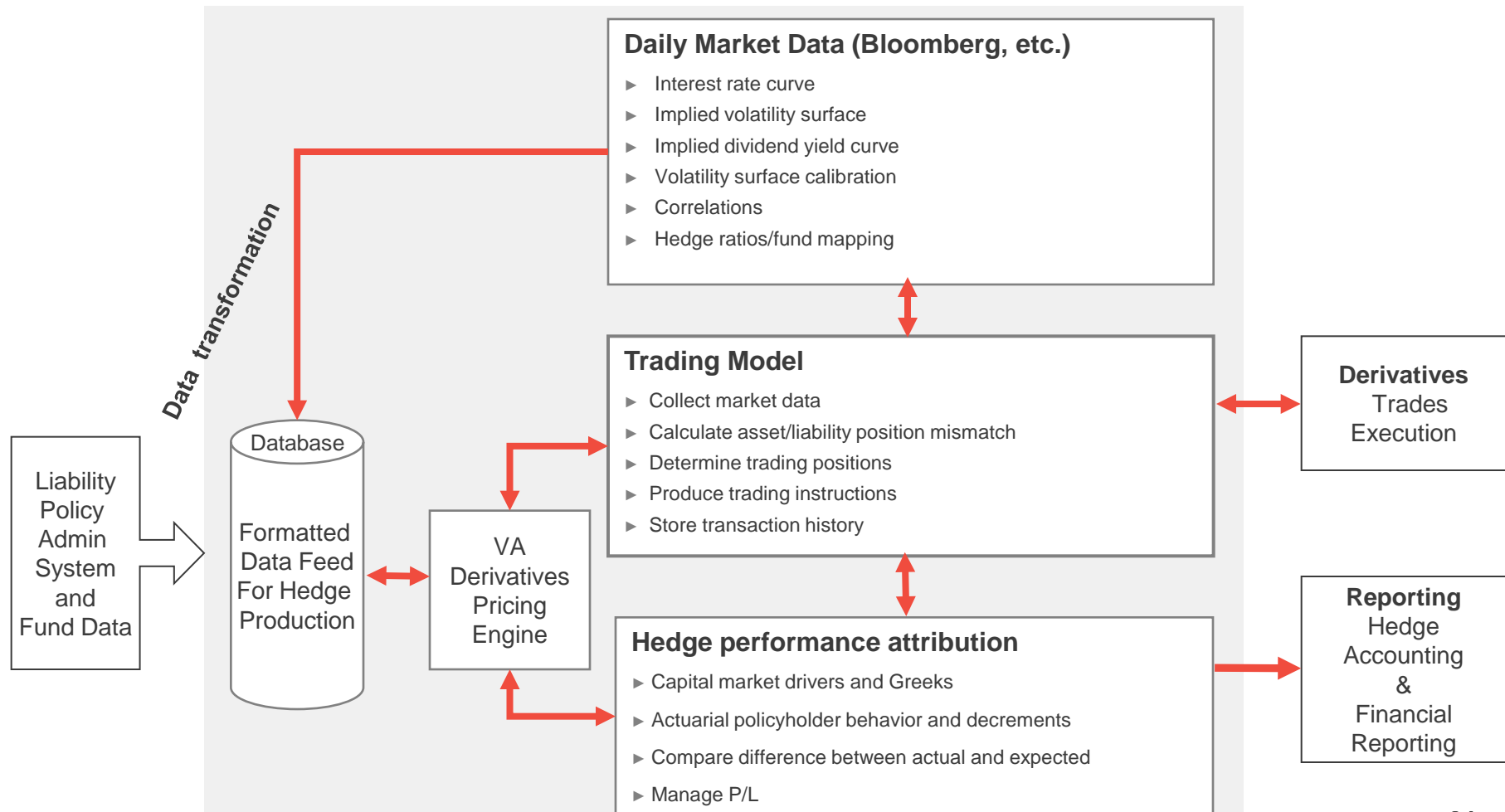
- ⇒ Risk neutral valuation of derivatives ensures consistent results
- ⇒ No matter what happens - real world or risk neutral path or good/bad scenario
- ⇒ Without taking any bets of market directions

***Hedging is to create opposite economic payoffs of the liability guarantees***

- *Through matching the sensitivities (Greeks) of the VA/FIA*
- *Greeks are capital market drivers of equity, interest rates, volatility, etc.*

# A dynamic hedging program (a “trading book”)

- There may be hundreds of thousands or millions of derivatives contracts in a book
- No closed form solutions but stochastic simulations for path dependent, long-dated, and basket options in VA book.
- Need very large computing grid for overnight simulation runs
- Maybe active derivatives trading to hedge the Greeks





# Financial engineering and actuarial science

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- ❑ **Law of large numbers does not work effectively with derivatives**
  - ⇒ Capital market risks are now dominate risks in many life insurance companies
  
- ❑ **Law of one number is critical for insurance derivatives products**
  - ⇒ Derivative contracts will be priced and risk is mitigated individually (not by average)
  - ⇒ Derivatives are priced with no-arbitrage and risk neutral hedging replication
  - ⇒ Dynamic hedging is used to manage the derivatives risks sold
  
- ❑ **Variable annuities and many current life insurance products need both law of large numbers and law of one numbers**
  - ⇒ New practice requires both financial engineering and actuarial science
  - ⇒ The non-market components are somewhat diversifiable
  - ⇒ Capital market derivatives exposure long dated and path dependent
  - ⇒ Imperfectly defined derivatives with many moving parts
  - ⇒ New practical and theoretical challenges and opportunities

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# Critical skills, education and knowledge needed

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## ❑ Actuarial exams and actuarial internship experience

- ⇒ Entry level job typically require 1-3 actuarial exams
- ⇒ Actuarial internship experience before graduation extremely helpful
- ⇒ Communication skills very helpful

## ❑ Risk management and investment actuaries

- ⇒ Advanced degree can be helpful
- ⇒ Option pricing, financial mathematics, investment
- ⇒ Computer programming (C++, C#, JAVA, VBA)

## ❑ Major advantage with actuarial science education

- ⇒ Mathematics, statistics, accounting, finance, computing
- ⇒ Most efficient education option with preparation for actuarial exams

# Where do life actuaries work

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## ❑ Mostly in life insurance or reinsurance companies

- ⇒ Most work as pricing and valuation actuaries
- ⇒ Large companies have formal or informal actuarial rotation program
- ⇒ Actuaries are supported with actuarial study time during work days
- ⇒ Actuaries are paid exam raises, in addition to annual salary increases
- ⇒ Some companies CEOs are actuaries

## ❑ Some in actuarial consulting

- ⇒ Actuarial insurance consulting firms
- ⇒ Actuarial auditing (Big Four Accounting Firms)
- ⇒ Life, benefit, health insurance, and pension consulting firms

## ❑ Few in investment bank

- ⇒ Portfolio management with insurance companies
- ⇒ Insurance related securitization
- ⇒ M&A transactions
- ⇒ Derivatives and trading

***Actuaries are mathematicians who work in business to solve world's problems!***



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